

Ch-4

Moving charges and Magnetism

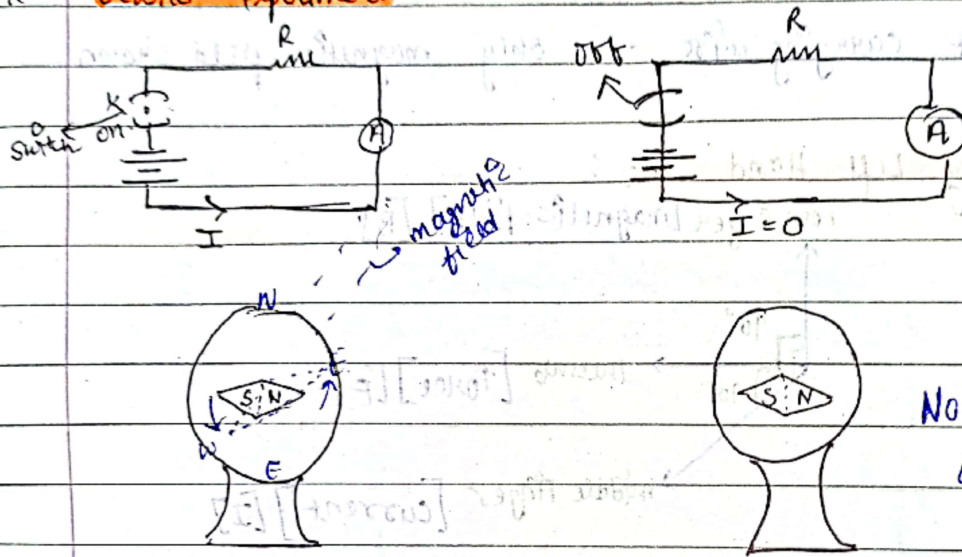
Electrodynamics
[charge is in motion]

Phenomenon of attraction b/w ferrous material & magnet.

* Compass Needle :

→ it is also called as bar magnet.

* Dested experiment



Movement of compass needle

→ N-pole → Towards west

S-pole → Towards east

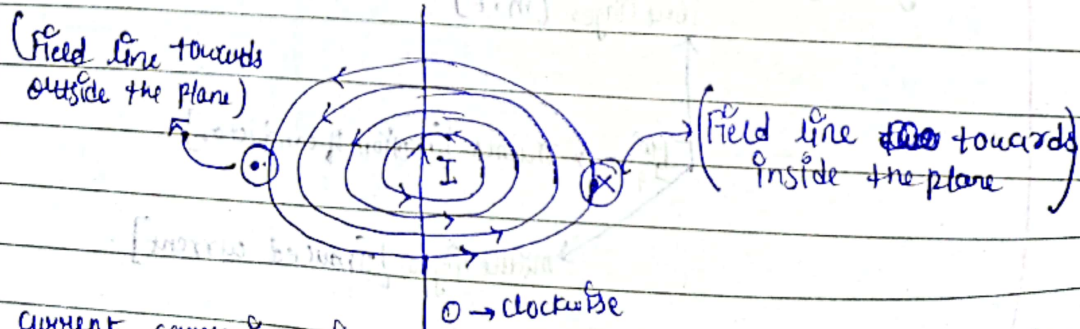
⇒ Anti-clockwise.

No deflection of compass needle

because there is no flow of current.

- Current carrying wire : contain magnetic field around conductors.

* Right hand thumb rule ^{observer}



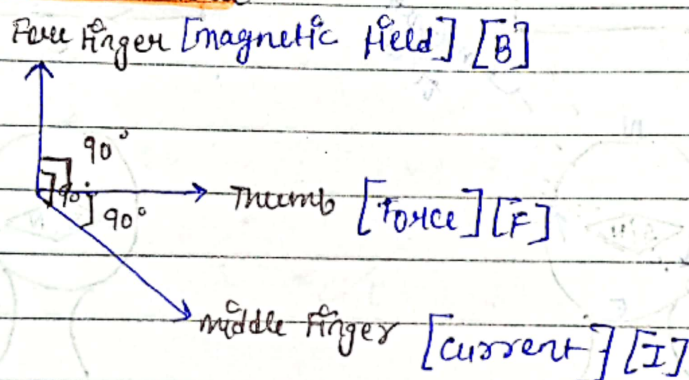
- current carrying wire form magnetic field

Thumb : direction of current
Fingers : direction of magnetic field.

⇒ A current or a field [electric or magnetic] emerging out of the plane of the paper is depicted by a dot $[\odot]$. A current or a field going into the plane of the paper is depicted by a cross $[\otimes]$.

- Due to charge → electric field is shown
- Due to moving charge → electric as well as magnetic field is shown
- Current carrying wire → only magnetic field shown.

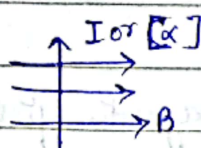
* Fleming Left Hand Rule :



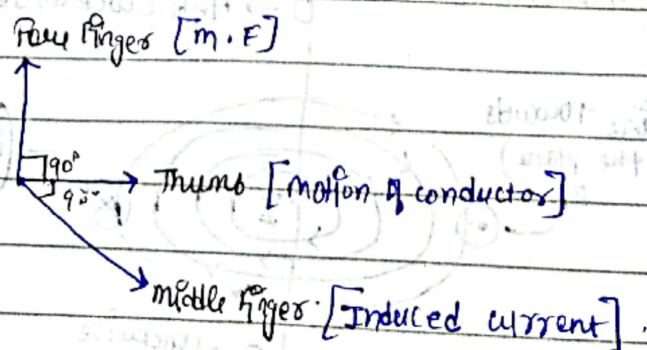
⇒ Application :

- Electric motor
- washing machine
- Fan.

⇒ Note :

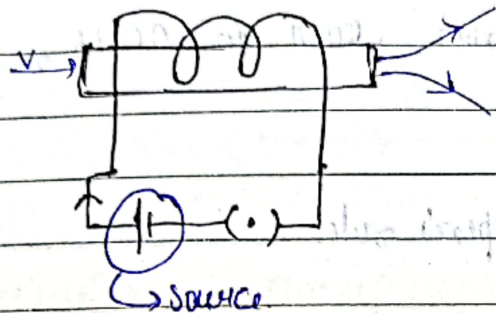


* Fleming Right Hand Rule :

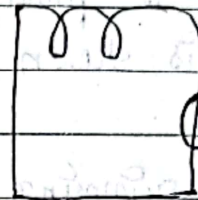


⇒ Application.

- Electric generator
- Transformer
- Mutual Induction.

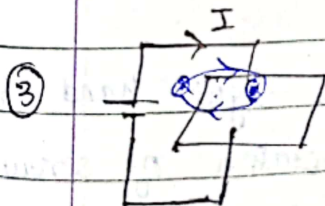
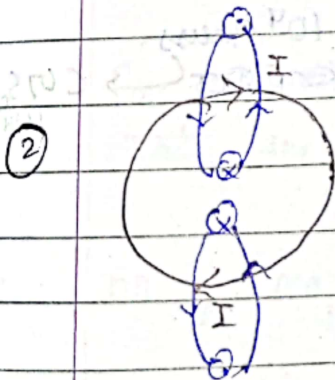
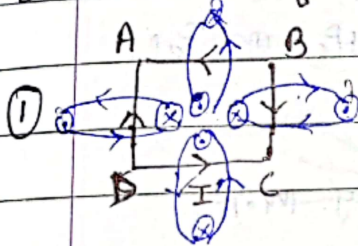


• Primary coil



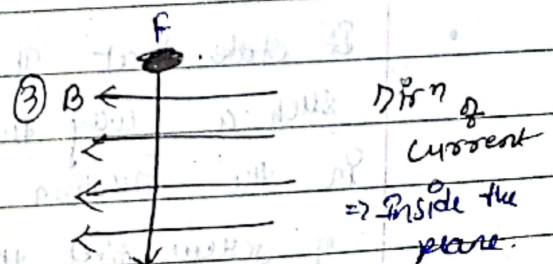
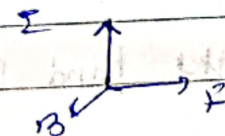
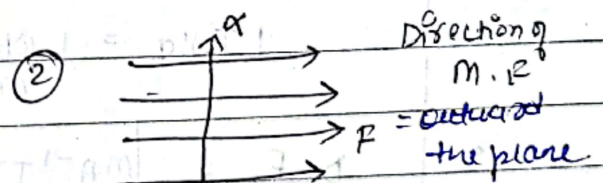
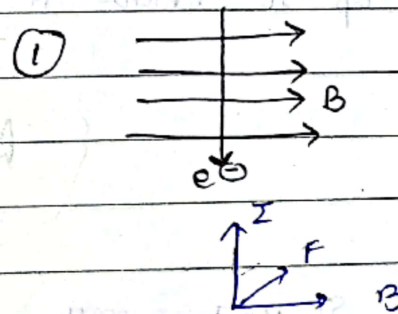
• Secondary coil

Q Find Dirⁿ of magnetic field.



Q Find Dirⁿ of Force

= inside the plane



*

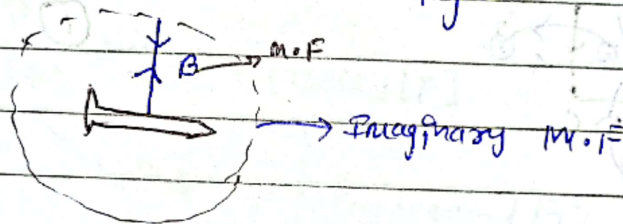
Oersted Experiment

- Oersted experiment: Oersted observed that if magnetic needle is placed near a current carrying wire the needle shows deflection for a moment.
- If current is flowing from South to North, the west deflection is shown.
- Also it's a swimming Ampere's rule.

*

Magnetic field

- The space around the current carrying wire or conductor up to which it can attract magnetic material.



- SI unit = Tesla

$$1 \text{ Tesla} = 1 \frac{\text{wb}}{\text{m}^2} \rightarrow \text{MKS unit}$$

$$1 \text{ T} = 10^4 \text{ gauss}$$

$$1 \text{ Gauss} = 10^{-4} \text{ T} \rightarrow \text{CGS unit}$$

$$B \cdot F = [M A^{-1} T^{-2}]$$

*

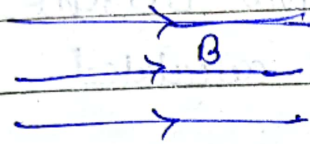
Right hand Thumb rule / Maxwell Rule

- It states that if we hold the screw in right hand in such a way that the direction of rotation of screw is in the direction of current then the direction of motion of screw gives the direction of magnetic field.

⊗ Indicates m.f inside

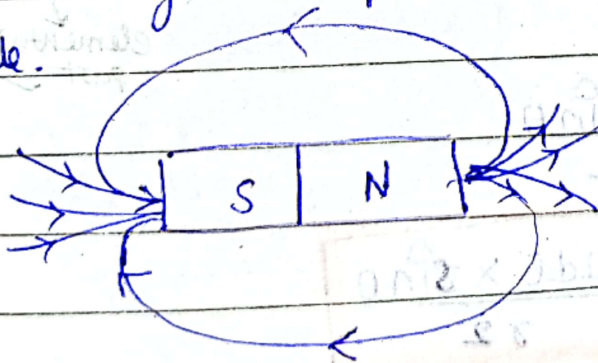
⊙ Indicates m.f outside

9. m.f lines are straight & parallel. It is called uniform m.f lines.



Properties of magnetic field lines.

magnetic field lines are imaginary & close loop.
m.f lines originate from north pole & merge into south pole.



Two magnetic lines never intersect each other.
~~Inside~~ the direction of magnetic field lines inside the magnet is south to north.
no. of magnetic field lines $\propto$ magnetic strength.

* Biot - Savart law

- According to this law, the magnetic field, magnitude at any point due to current element depends directly upon current element $[Idl]$, $\sin$ of angle θ , inversely upon to square of distance b/w current & point where the magnitude of magnetic field calculated.

$$\Rightarrow dB \propto Idl \quad \text{--- (1)}$$

$$\Rightarrow dB \propto \sin \theta \quad \text{--- (2)}$$

$$\Rightarrow dB \propto \frac{1}{r^2} \quad \text{--- (3)}$$

considering eqn (1), (2), & (3)

$$dB \propto \frac{Idl \sin \theta}{r^2}$$

$$dB = \frac{\mu_0}{4\pi} \frac{Idl \sin \theta}{r^2}$$

$\rightarrow$ Permittivity in free space [vacuum]

$$\int dB = \frac{\mu_0 I \sin \theta}{4\pi r^2} \int dl$$

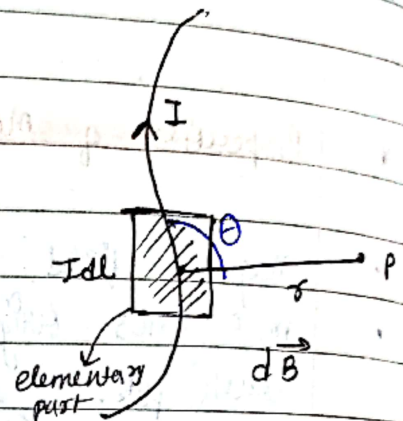
$$\frac{\mu_0}{4\pi} = 10^{-7} \text{ Tm/A}$$

- In vector form

$$\vec{dB} = \frac{\mu_0}{4\pi} \frac{Idl \sin \theta}{r^2} \hat{r}$$

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{Idl \sin \theta}{r^3} \vec{r}$$

$$\left[\hat{r} = \frac{\vec{r}}{r} \right]$$



$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{[d\vec{l} \cdot \vec{r} \sin\theta]}{r^3}$$

$$d\vec{B} = \frac{\mu_0 I}{4\pi r^3} [d\vec{l} \times \vec{r}]$$

case I

$$\theta = 0^\circ$$

$$[d\vec{B} = 0]$$

$\hookrightarrow d\vec{l}$ is parallel to $\vec{r}$

case II

$$\theta = 90^\circ$$

$$dB = \frac{\mu_0 I dl}{4\pi r^2}$$

Ex *

Dimensional formula of permeability $[\mu_0]$

$$d\vec{B} = \frac{\mu_0 I dl \sin\theta}{4\pi r^2}$$

$$\mu_0 = \frac{dB \times r^2}{(I) dl}$$

$$= \frac{T \cdot l^2}{A \times l}$$

$$= T L A^{-1}$$

$$= [M A^{-1} T^{-2} A^{-1} L]$$

$$= [M L T^{-2} A^{-2}]$$

Ex 4.4

$$I = 10A$$

$$\Delta x = 1cm$$

$$0.01$$

$$r = 0.5m$$

$$\Delta l = \Delta x \hat{i}$$

$$dB = \frac{\mu_0 I dl \sin\theta}{4\pi r^2} \quad \sin\theta = 1$$

$$= \frac{10^{-7} \times 10 \times 10^{-2}}{25 \times 10^{-2}}$$

$$= 4 \times 10^{-8} T$$

* Application of Biot-Savart law

Application of Biot-Savart law

- Expression of magnetic field for circular current carrying wire

We know,

$$dB = \frac{\mu_0}{4\pi} \frac{Idl \sin\theta}{r^2} \quad [\text{Biot-Savart's law}]$$

$$\theta = 90^\circ$$

$$\int_0^L dB = \frac{\mu_0}{4\pi} \frac{I}{r^2} \int_0^L dl$$

$$B = \frac{\mu_0}{4\pi} \times \frac{I}{r^2} \left[l \right]_0^L$$

$$B = \frac{\mu_0 I \cdot L}{4\pi r^2}$$

$$L = 2\pi r \quad [\text{circumference}]$$

$$B = \frac{\mu_0 I}{4\pi r^2} \times 2\pi r$$

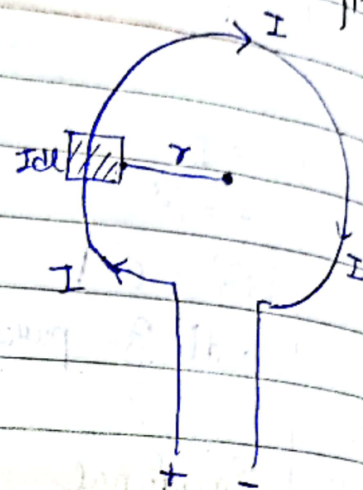
$$B = \frac{\mu_0 I}{2r}$$

→ For semi-circular loop.

$$l = \frac{2\pi r}{2} = \pi r$$

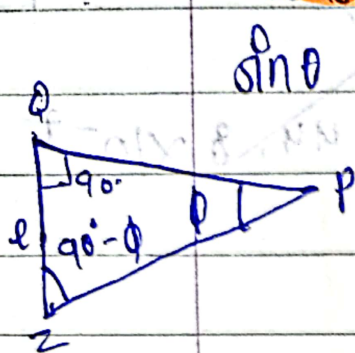
→ For quadrant-circular loop.

$$l = \frac{2\pi r}{4} = \frac{\pi r}{2}$$



*

Magnetic field due to a long straight current carrying conductor.



$$\sin \theta = \sin [90 - \phi] \quad \tan \phi = \frac{l}{a}$$

$$= \cos \phi$$

$$l = a \tan \phi$$

$$(dl = a \sec^2 \phi d\phi)$$

$$+\phi_2 = \text{CW}$$

$$-\phi_1 = \text{ACW}$$

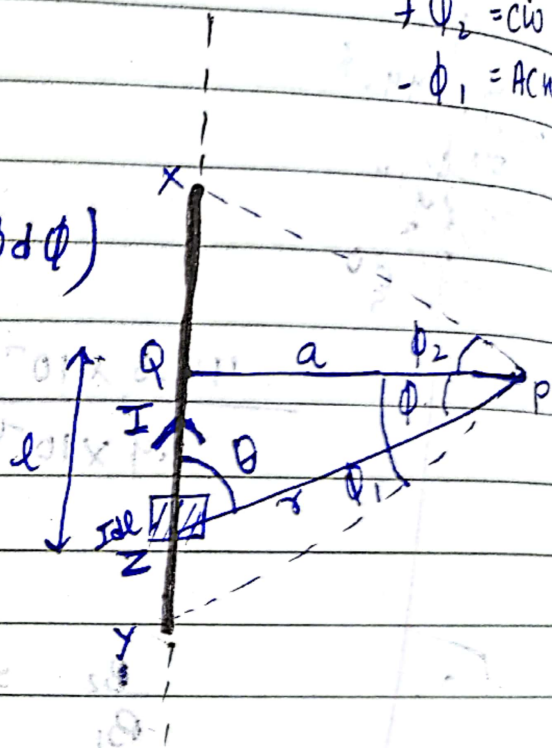
we know,

$$dB = \frac{\mu_0}{4\pi} \frac{I dl \sin \theta}{r^2}$$

$$dB = \frac{\mu_0 I}{4\pi} \frac{a \sec^2 \phi d\phi \times \cos \phi}{\left(\frac{a}{\cos \phi}\right)^2}$$

$$dB = \frac{\mu_0 I}{4\pi} \frac{\cancel{a} \sec^2 \phi \cdot \cos \phi d\phi}{a \cancel{r} \times \sec^2 \phi}$$

$$dB = \frac{\mu_0 I}{4\pi a} \int_{-\phi_1}^{+\phi_2} \cos \phi d\phi$$



Integrating both side.

$$\int dB = \frac{\mu_0 I}{4\pi a} \int_{-\phi_1}^{+\phi_2} \cos \phi d\phi$$

$$B = \frac{\mu_0 I}{4\pi a} [\sin \phi]_{-\phi_1}^{\phi_2}$$

$$B = \frac{\mu_0 I}{4\pi a} [\sin(\phi_2) - \sin(-\phi_1)] \quad \left[\because \sin(-\theta) = -\sin \theta \right]$$

$$B = \frac{\mu_0 I}{4\pi a} [\sin(\phi_2) + \sin(\phi_1)]$$

Case I,

$\phi_1 = \phi_2 = \phi$ [symmetrical wire] [axis bisect the conducting wire].

$$B = \frac{\mu_0 I}{4\pi a} [\sin \phi + \sin \phi]$$

$$B = \frac{1}{2} \frac{\mu_0 I}{2\pi a} \sin \phi$$

$$B = \frac{\mu_0 I}{2\pi a} \sin \phi$$

Case II

$$\phi_1 = \phi_2 = \sin^{-1} \frac{a}{r}$$

$$B = \frac{\mu_0 I}{2\pi a} \times \sin \sin^{-1} \frac{a}{r}$$

$$B = \frac{\mu_0 I}{2\pi a} \times \frac{1}{\sqrt{2}}$$

$$B = \frac{\sqrt{2} \cdot \mu_0 I}{4\pi a}$$

Case III

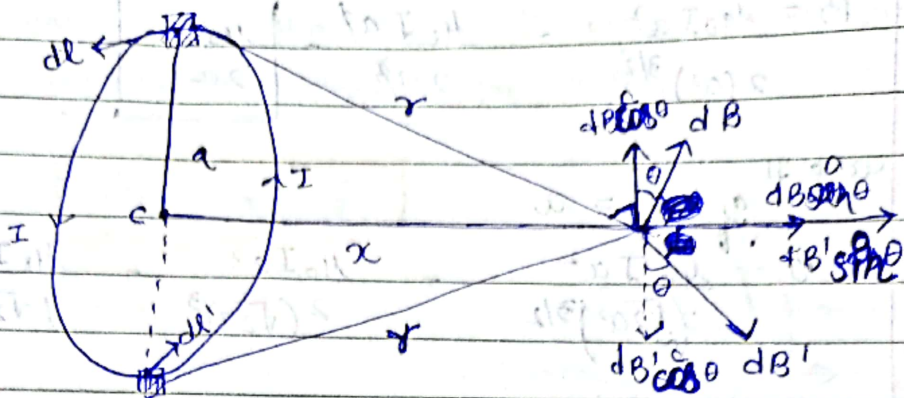
$$\phi_1 = 0 \quad \phi_2 = \sin^{-1} \frac{a}{r}$$

$$B = \frac{\mu_0 I}{4\pi a} [\sin \sin^{-1} \frac{a}{r} + 0]$$

$$B = \frac{\mu_0 I}{4\pi a} \times \frac{1}{\sqrt{2}}$$

$$B = \frac{\sqrt{2} \mu_0 I}{8\pi a}$$

* Magnetic field on the axis of a circular current loop.



$$dB = \frac{\mu_0 I dl \sin \theta}{4\pi r^2}$$

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{[d\vec{l} \times \vec{r}]}{r^3}$$

$$dB = dB' \sin \theta$$

$$\int dB = \int dB' \sin \theta$$

$$\int dB = \int dB' \sin \theta$$

$$B = \int_0^L \frac{\mu_0 I dl' \sin \theta}{4\pi r^2} \quad \left[\sin \theta = \frac{a}{r} \right]$$

$$B = \frac{\mu_0 I a}{4\pi r^3} \int_0^{2\pi} dl$$

$$B = \frac{\mu_0 I a}{4\pi r^3} \times 2\pi a$$

$$B = \frac{\mu_0 I a^2}{2r^3}$$

$$r = \sqrt{x^2 + a^2}$$

$$B = \frac{\mu_0 I a^2}{2r^3}$$

$$B = \frac{\mu_0 I a^2}{2(x^2 + a^2)^{3/2}}$$

case I

∴ q point lies on centre.

$$x = 0$$

$$B = \frac{\mu_0 I a^2}{2(a^2)^{3/2}} = \frac{\mu_0 I a^2}{2a^3} = \boxed{\frac{\mu_0 I}{2a}}$$

case II

$$q_1 \quad x = a$$

$$B = \frac{\mu_0 I a^2}{2(\sqrt{2}a)^{3/2}} = \frac{\mu_0 I a^2}{2(\sqrt{2}a)^3} = \frac{\mu_0 I a^2}{4\sqrt{2}a^3}$$

$$\boxed{B = \frac{\mu_0 I}{4\sqrt{2}a}}$$

4.6

$$N = 100 \quad r = \frac{10 \text{ cm}}{100}$$

$$I = 1 \text{ A}$$

$$B = \frac{\mu_0 N I}{2R} = \frac{4\pi \times 100 \times 10^{-2} \times 1}{2 \times 10^{-1}}$$

$$= 2 \times 10^2 \times 10^{-2} \times 10$$

$$= 2\pi \times 10^{-4}$$

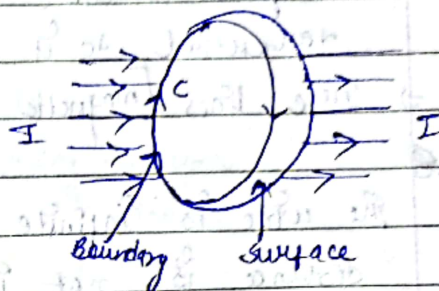
$$= 2 \times 3.14 \times 10^{-4} \text{ T}$$

$$= 6.28 \times 10^{-4} \text{ T}$$

* Ampere's Circuital law

This law states that the $\oint \mathbf{B} \cdot d\mathbf{l}$ is equal to μ_0 times of total current passing through the surface.

$$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 i$$

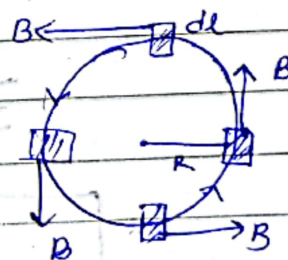


⇒ Important points of Ampere's Circuital law

- $\mathbf{B}$ is tangential to the surface & $\mathbf{B}$ is non-zero
- $\mathbf{B}$ is normal to the loop.
- $\mathbf{B}$ vanishes.

⇒ Application

magnetic field of circular loop



we know that

$$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 i$$

$$\oint B \times dl \cos \theta = \mu_0 i \quad [\theta = 0^\circ]$$

$$B \oint dl = \mu_0 i$$

$$B \times 2\pi r = \mu_0 i$$

$$B = \frac{\mu_0 i}{2\pi R}$$

$$B = \frac{N \mu_0 I}{2\pi R}$$

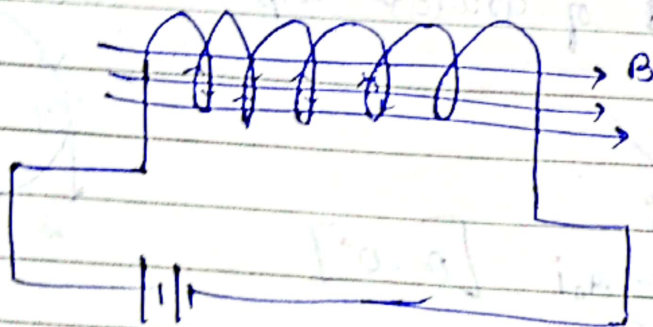
→ for N no. of turns.

2) Field of infinitely long wire

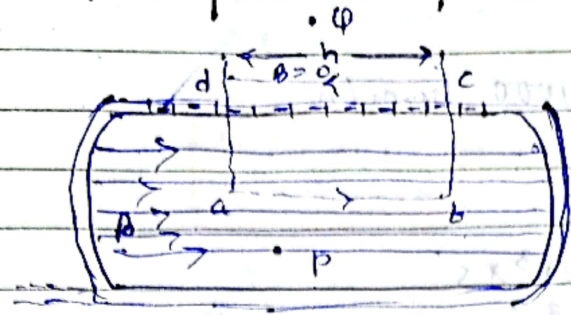
- It implies that the field at every point on a circle of radius r , [with the wire along the axis] is same in the magnitude.
- The field direction at any point on the circle is tangential to it.
- These lines [magnetic field] forms close loop.
- As wire is infinite, the field due to it at non-zero distance is not infinite. [$R \rightarrow \infty$].
- Grasp the wire in your right hand with your extended thumb pointing in the direction of the current. Your fingers will curl around in the direction of the magnetic field.

* Solenoid

- It consists of a long wire wound in the form of a helix where the neighbouring turns are closely spaced.



Magnetic field of solenoid for N no. of turns.



B = magnetic field.
 I = current passing through
 n = No. of turns per unit length

$$n = \frac{N}{l}$$

l = length of wire.

loop [rectangular ABCDA]
 Magnetic field of side 'AB' $[B_{AB}] = \oint_A^B B \cdot dL \cos \theta = \int_A^B B \cdot dl$
 " " " " 'BC' $[B_{BC}] = \oint_B^C B \cdot dL \cos 90^\circ = 0$

$$B_{net} = B \cdot \int_0^h dl$$

$$\mu_0 I = B \cdot h$$

$$\frac{\mu_0 I}{h} = B$$

For 'N' no. of turns
 $B = \frac{\mu_0 I N}{h}$

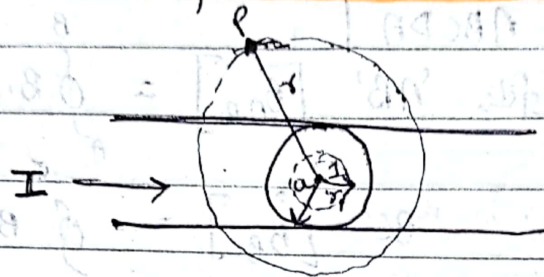
$$B = \frac{\mu_0 I n}{h}$$

$$B = \mu_0 I n$$

no. of turns / m

Ex 4.8

Figure shows a long straight wire of a circular cross-section [radius a] carrying steady current I . The current I is uniformly distributed across this cross-section. Calculate the magnetic field in the region $r < a$ and $r > a$.



(i) $r < a$

(ii) $r = a$

(iii) $r > a$

$\hookrightarrow B = \frac{\mu_0 I}{2\pi a}$

At point 'p'

$L = 2\pi r$

$\oint B \cdot dL = \mu_0 I$

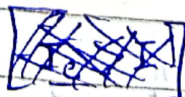
$B \cdot 2\pi r = \mu_0 I$

$B = \frac{\mu_0 I}{2\pi r}$

$\left[B \propto \frac{1}{r} \right]$

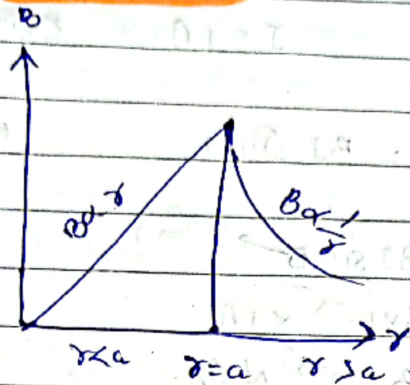
$I_e = \frac{I(\pi r^2)}{\pi a^2}$

$I_e = \frac{I r^2}{a^2}$

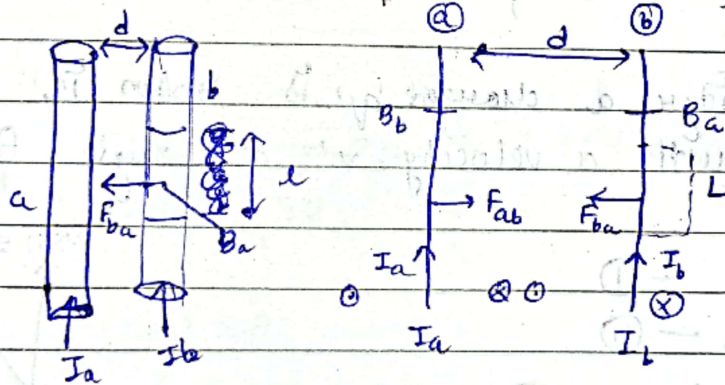


$$B = \frac{\mu_0 I_e}{2\pi r} = \frac{\mu_0 I r^{\cancel{x}}}{2\pi \cancel{r} a^2}$$

$$B = \frac{\mu_0 I r}{2\pi a^2} \quad (B \propto r)$$



* Force Between Two parallel currents, The Ampere



Acc. to Ampere circuital law,

$$B_a = \frac{\mu_0 I_a}{2\pi d} \quad \text{--- (i)}$$

Magnetic force on wire 'b'
 $F_{ba} = BIL \sin \theta \quad [\theta = 90^\circ]$

$$F_{ba} = B_a I_b L \quad \text{--- (ii)}$$

Putting value 'B_a' in eq (ii)

$$F_{ba} = \frac{\mu_0 I_a}{2\pi d} \times I_b \cdot L$$

$$F_{ba} = \frac{\mu_0 I_a I_b \times L}{2\pi d}$$

Force per unit length $\left(\frac{F_{ba}}{L}\right)$

$$F = \frac{\mu_0 I_a I_b}{2\pi d}$$

Ex 4.9

$$B = 3 \times 10^{-5} \text{ T}$$

$$I = 1 \text{ A}$$



$$(a) \quad f = \left(\frac{F}{L}\right) = BI \sin \theta$$

$$(b) \quad \theta = 0^\circ$$

$$f = 0$$

$$f = BI \sin \theta \rightarrow 90^\circ = 1$$

$$= 3 \times 10^{-5} \times 1 \text{ A}$$

$$= 3 \times 10^{-5} \text{ N/m}$$

* Motion in a magnetic field

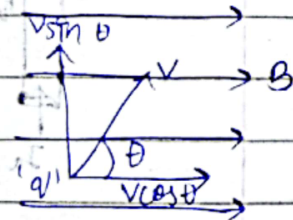
Let us consider a charged 'q' is thrown in uniform magnetic field 'B' with a velocity 'v' at angle θ

$$F \propto q \quad \text{--- (i)}$$

$$F \propto B \quad \text{--- (ii)}$$

$$F \propto v \sin \theta \quad \text{--- (iii)}$$

Combining eqn (i), (ii) & (iii)



$$F \propto q \cdot v \cdot B \sin \theta$$

$$F = K q \cdot v \cdot B \sin \theta \quad [K=1]$$

$$F = q [v B \sin \theta]$$

Scalar form

$$\vec{F} = q (\vec{v} \times \vec{B})$$

Vector form

Case I

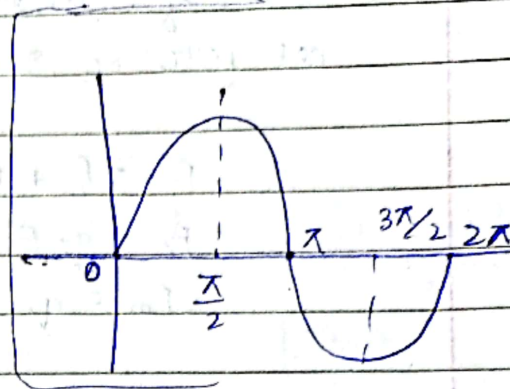
If charged particle is thrown antiparallel to uniform magnetic field.

$$\theta = 180^\circ$$

$$F = q \cdot v \cdot B \sin \theta$$

$$F = q \cdot v \cdot B \times 0$$

$$\boxed{F = 0}$$



Case II

$$v \parallel B$$

$$\theta = 0^\circ$$

$$\boxed{F = 0}$$

Case III

If a charged particle is held stationary uniform magnetic field.

$$v = 0$$

$$F = q \cdot v \cdot B \sin \theta$$

$$\boxed{F = 0}$$

Case IV

Max^m Magnitude of Force.

$$\theta = 90^\circ$$

$$\boxed{F = q \cdot v \cdot B}$$

$$\boxed{F = \frac{E}{v} \times vB} \quad \left[\begin{array}{l} v = \frac{W}{q} = \frac{E}{q} \\ q = \frac{E}{\text{volt}} \end{array} \right]$$

v = potential difference

E = Energy

v = velocity of charge particle

*

Lorentz force

The sum of electrostatic force and magnetic force represent the net force on moving charged particle.

$$F = F_e + F_m \quad \text{--- (I)}$$

$$F_e = qE \quad \text{--- (II)}$$

$$F_m = q \cdot [\vec{v} \times \vec{B}] \quad \text{--- (III)}$$

Put F_e & F_m in eqn (I)

$$F = [qE + q \cdot \vec{v} \times \vec{B}]$$

$$F = q [\vec{E} + \vec{v} \times \vec{B}]$$

$$F = q [E + vB \sin \theta]$$

Case I

$$\theta = 0^\circ$$

$$F = F_e$$

$$F = qE$$

Case II $\theta = 90^\circ$

$$F = qE + qvB$$

Case III

$$F = 0$$

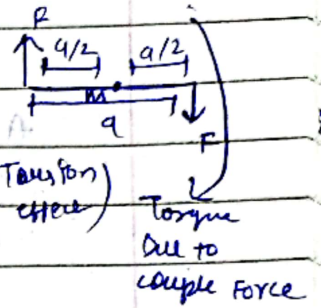
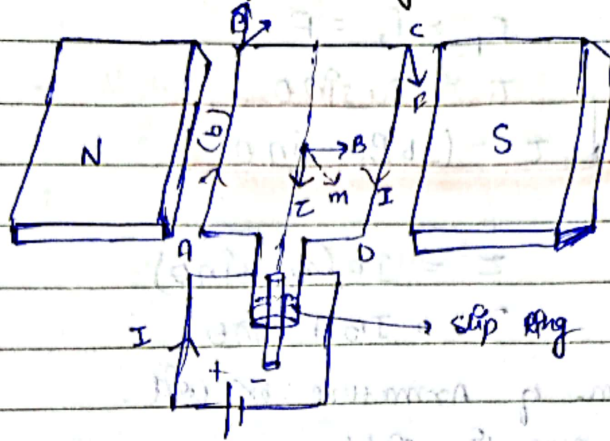
$$0 = qE + qvB$$

$$-q \cdot vB = -qE$$

$$B = \frac{|E|}{|v|}$$

$$v = \frac{-|E|}{|B|}$$

Torque on a current loop, magnetic dipole.



Boundary condition.

$$F_1 = F_2 = (Ib)B$$

moment about 'm' due to F_1

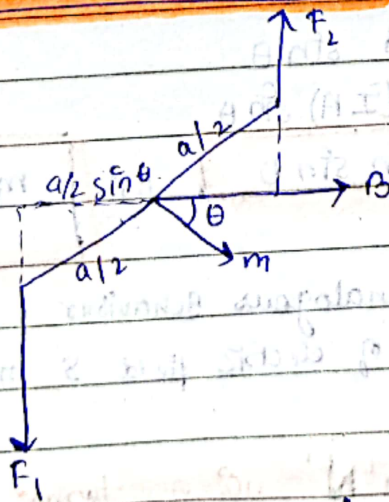
$$M_m = F_1 \times \frac{a}{2}$$

Due to F_2

$$M_m = F_2 \times \frac{a}{2}$$

$$\tau = M_m(F_1) + M_m(F_2)$$

$$\tau = F_1 \frac{a}{2} + F_2 \frac{a}{2}$$



$$M_m(F_2) = F_2 \cdot \frac{a}{2} \sin \theta$$

$$M_m(F_1) = F_1 \cdot \frac{a}{2} \sin \theta$$

$$\begin{aligned} \tau &= M_m(F_1) + M_m(F_2) \\ &= F_1 \frac{a}{2} \sin \theta + F_2 \frac{a}{2} \sin \theta \end{aligned}$$

$$F = (Ib)B$$

$$F_1 = F_2 = F$$

$$\tau = F a \sin \theta$$

$$\tau = (Ib)Ba \sin \theta$$

$$\tau = IB(ab) \sin \theta$$

$$\tau = IBA \sin \theta$$

A = Area of Armature or coil.

B = magnetic field.

I = current

τ = Torque on coil.

* Magnetic Moment

1) The product of electric current and cross-sectional area of coil and armature [Area-vector].

$$m = IA$$

$$\text{unit : } A \cdot m^2$$

$$\tau = IBA \sin \theta$$

$$\tau = B(IA) \sin \theta$$

$$\tau = B \cdot m \sin \theta$$

OR

$$m = \frac{\tau}{B \sin \theta}$$

$$\tau = B \cdot m$$

$$\tau = E \cdot E$$

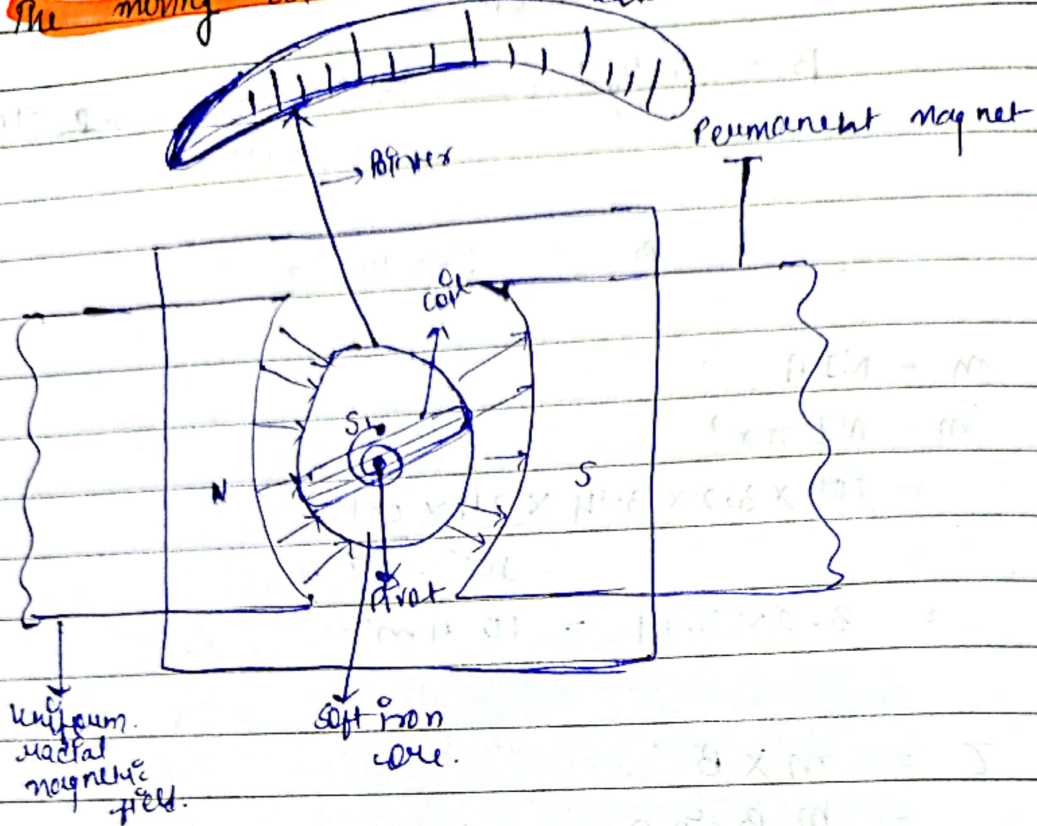
→ analogous behaviour
of electric field & m.f

2) magnetic moment for 'N' no. of turns

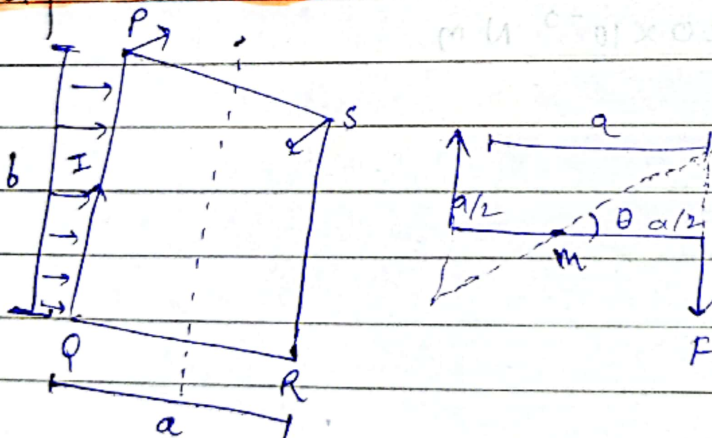
$$m = NIA$$

$$\tau = NIBA \sin \theta$$

* The moving coil galvanometer.



Working & calculation



$$\tau = F \cdot \frac{a}{2} \sin \theta + F \cdot \frac{a}{2} \sin \theta$$

$$= 2F \cdot \frac{a}{2} \sin \theta$$

$$\tau = F \cdot a \sin \theta \rightarrow 90^\circ = 1$$

$$F = NBIL$$

$$F = NBIb$$

$$\tau = f \cdot a \sin \theta$$

$$\tau = NBI (ba) \sin \theta$$

$$\tau = NBI A \sin \theta$$

$A = ba$
 $\rightarrow$ Area of armature.

$$I = \frac{\tau}{NBA \sin \theta}$$

For $\theta = 90^\circ$

$$I = \frac{\tau}{NBA}$$

* For deflection / sensitivity

$$\tau = k \alpha = NIBA$$

$$\alpha = \frac{NIBA}{k}$$

$k \rightarrow$ Torsional constant

$\alpha =$ angular deflection

* Factor on which the sensitivity of moving coil galvanometer depends.

1) No. of turns $[N]$

2) Magnetic field $[B]$

3) Area of coil $[A]$

4) Torsional constant $[k]$

Q. A rectangular coil having each turn of length 5 cm and breadth 2 cm is suspended freely in a radial magnetic field of induction $2.5 \times 10^{-2} \text{ Wb/m}^2$. K of suspension fibre is $1.5 \times 10^{-8} \text{ Nm/rad}$. The coil deflect through the angle of 1.2 radian when current flow 2 mA . Find the no. of turns? $\rightarrow 2 \times 10^{-6} \text{ A}$

$$N = \frac{k \alpha}{I B A}$$

$$N = \frac{1.5 \times 10^{-8} \times 1.2 \times 10^3}{2 \times 10^{-6} \times 2.5 \times 10^{-2} \times 0.1} = \frac{1.5 \times 1.2 \times 10^{-4} \times 5}{2.5 \times 10^{-4}} = 3.6 \times 10^4$$

$$R = \frac{\pi}{180}$$

$$R = \frac{\pi}{180} \times 10$$

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Black sequence = 8, 12, 13, 14

* Voltage sensitivity

$$V_s = \frac{\theta}{V} = \frac{\theta}{IR} = \frac{NIBA}{KIR}$$

$$V_s = \frac{NBA}{KR} \rightarrow \text{Resistance}$$

* Current sensitivity

$$I_s = \frac{NBA}{K}$$

Q To increase the current sensitivity of a moving coil galvanometer by 50%, its resistance is increased so that the new resistance becomes twice its original resistance by what factor does its voltage sensitivity change

	Initial	Final
I_s	100	150
R	"	"

$$\frac{150}{100} = \frac{3}{2}$$

$$\text{Ratio} = 3 : 2$$

$$A = 6 \times 10^{-4} \text{ m}^2$$

$$N = 60$$

$$\alpha = 18^\circ$$

$$I = 0.20 \text{ mA} \rightarrow 10^{-3}$$

$$B = 90 \text{ G} = 9 \times 10^{-4} \text{ T}$$

$$K = ?$$

$$K = \frac{NIBA}{\alpha}$$

$$= \frac{60 \times 0.20 \times 10^{-3} \times 9 \times 10^{-4}}{5 \times 10^{-4}}$$

$$0.314$$

$$= \frac{5400 \times 10^{-11}}{3.14} = 1.7 \times 10^{-7} \text{ Nm/rad}$$

